

**ATOMIC ENERGY EDUCATION SOCIETY, MUMBAI**

**CLASS: XII (MATHS)**

**WORKSHEET: MODULE 1/4**

**CHAPTER-5**

**TOPIC: CONTINUITY AND DIFFERENTIABILITY**

Q1. Find the value of k, for which  $f(x) = \begin{cases} \frac{\sqrt{1+kx}-\sqrt{1-kx}}{x} & , \text{if } -1 \leq x < 0 \\ \frac{2x+1}{x-1} & , \text{if } 0 \leq x < 1 \end{cases}$  is continuous at

$x = 0$

Q2. Find the value of k, so that the function f defined by  $f(x) = \begin{cases} \frac{k \cos x}{\pi - 2x} & , \text{if } x \neq \frac{\pi}{2} \\ 3 & , \text{if } x = \frac{\pi}{2} \end{cases}$  is continuous at

$x = \frac{\pi}{2}$

Q3. Find the values of a and b such that the following function f(x) is a continuous function

$$f(x) = \begin{cases} 5 & x \leq 2 \\ ax + b & , 2 < x < 10 \\ 21 & , x \geq 10 \end{cases}$$

Q4. Find the value of a, if the function f(x) defined by  $f(x) = \begin{cases} 2x - 1 & , x < 2 \\ a & , x = 2 \\ x + 1 & , x > 2 \end{cases}$  is continuous at

$x = 2$

Q5. If f(x) defined by the following, is continuous at  $x = 0$ , then find the values of a, b and c

$$f(x) = \begin{cases} \frac{\sin(a+1)x + \sin x}{x} & , \text{if } x < 0 \\ c & \text{if } x = 0 \\ \frac{\sqrt{x+bx^2} - \sqrt{x}}{b(x)^{3/2}} & , \text{if } x > 0 \end{cases}$$

Q6. Show that  $f(x) = \begin{cases} 5x - 4 & , \text{when } 0 < x \leq 1 \\ 4x^3 - 3x & , \text{when } 1 < x < 2 \end{cases}$  is continuous at  $x = 1$

Q 7. Discuss the continuity of the function  $f(x) = \begin{cases} x^3 - 3 & , x \leq 2 \\ x^2 + 1 & , x > 2 \end{cases}$

Q8. Find the relation between a and b so that  $f(x) = \begin{cases} ax + 1 & , x \leq 3 \\ bx + 3 & , x > 3 \end{cases}$  is continuous at  $x = 3$ .

Q9. Show that the function defined by  $g(x) = x - [x]$  is discontinuous at all integral points.

Q10. Discuss the continuity of the function (i)  $f(x) = \frac{1}{x}$  (ii)  $f(x) = \frac{1}{|x-5|}$  (iii)  $f(x) = |x-5|$

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